

Homework 4

Due April 14, 1997

1. Green & Limebeer, Problem 5.2.

(Classical derivation of optimal control via calculus of variations.)

Hint: in Part 5, use the property stated in Problem 3.3(3).

You do not have to prove invertibility in Part 6.

2. Green & Limebeer, Problem 5.4.

HARD, but try to do as much as you can.

You do not have to give the three reasons asked in Part 1.

Hints:

- Use Theorem 3.2.1 in Part 2.
- In Part 3, use the version of bounded real lemma quoted in the Note on page 111.

Part 4 is crucial (and famous). It establishes robustness of optimal controllers. Sketch a Nyquist diagram and draw the phase and gain margin conclusions.

3. Green & Limebeer, Problem 5.5.

You do not have to discuss the existence of P_α in Part 1.

4. Green & Limebeer, Problem 5.14.

Important—practice the measurement feedback design from Section 5.4.