

# Optimization and Control of Advanced Automotive Engines

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Ford Research and Advanced Engineering

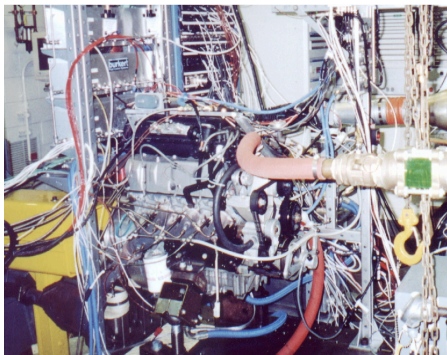
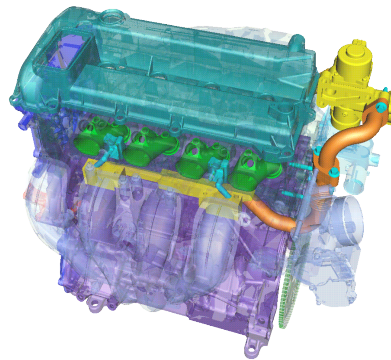
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## Acknowledgement:

S. Magner, I. Kolmanovsky, S. Cooper, D. Hagner, D. Popovic



Where, what, how, and why



## Modern vehicles are computerized machines ...

- Computers control practically everything:
  - **engine**, transmission
  - braking (ABS), traction
  - air-bags, power-windows, ...
- Engine computer control enabled
  - very low emissions by accurate of air/fuel control
  - **optimized** performance and **fuel economy** via addition of new devices.
- Optimization task different (more difficult) than set point regulation
  - obtaining accurate models expensive/time-consuming
  - complexity increases exponentially with each additional device.



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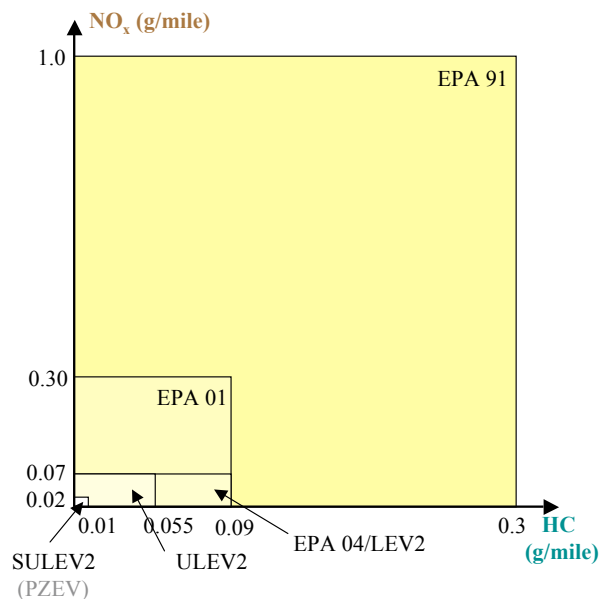
## Emissions

### Regulated tailpipe emissions (EPA and CARB)

- NMOG (HC)
- NO<sub>x</sub>
- CO
- particulates

### Steps to achieve high standards:

- large/multiple catalytic converters
- **control AF ratio at stoichiometry**
- special cold start strategies to speed up catalyst light-off.



A sample of emission regulations since 1991  
at 100/120 K miles.



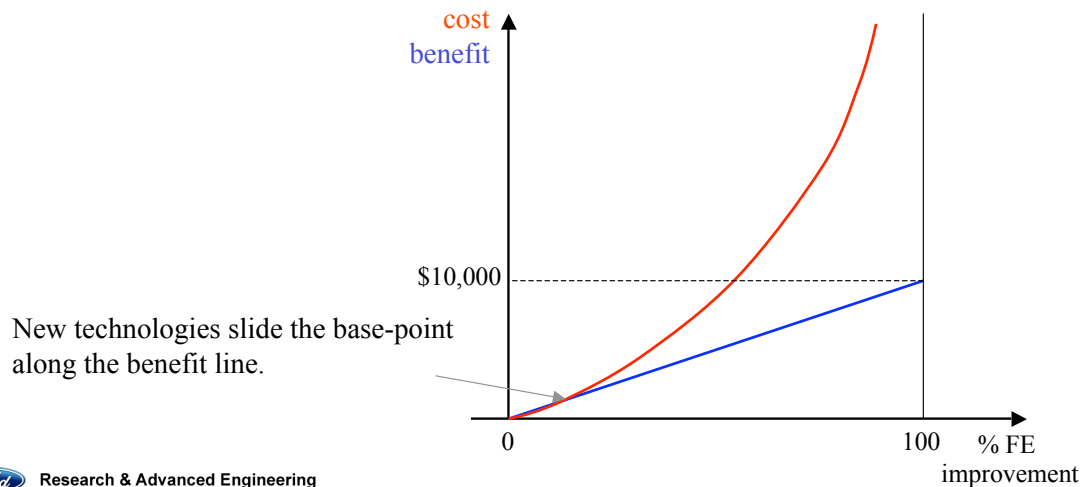
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## Fuel economy

Automakers must satisfy CAFE standard for fleet fuel economy:

- cars – 27.5 mpg
- light trucks – 20.7 mpg increasing to 22.2 mpg (model year 2007)

**Customer benefit** → average vehicle, driven 120K miles, at \$2/gallon gas:  
**\$100 per 1% FE improvement**



## Design for fuel economy

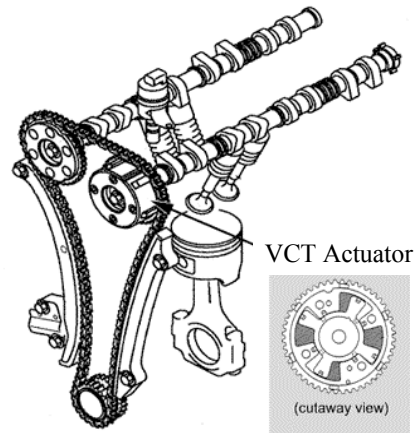
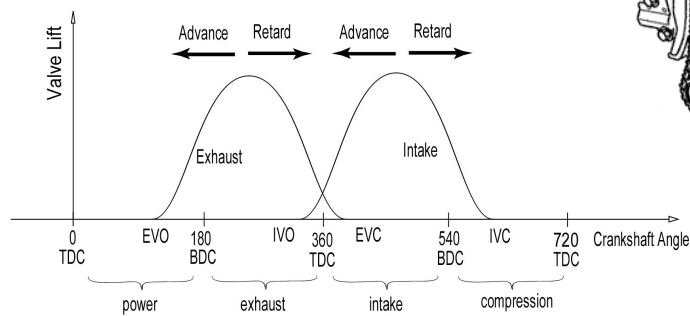
- Conventional **SI** (gasoline) engine
  - throttle controls air (**torque**)
  - fuel controlled to stoichiometric AF ratio (14.6)
  - spark for best fuel economy (MBT spark) → 1 DoF optimization
- New devices added/combined to improve FE:
  - **Camless** – 5 DoF:
    - intake and exhaust valve opening and closing times, spark timing.
  - **Lean burn** – 3 DoF:
    - air-fuel ratio, variable cam timing (VCT), spark timing
  - **Dual-independent VCT** – 3 DoF :
    - intake VCT, exhaust VCT, spark timing
    - [test platform for this work.](#)

## Dual-independent VCT engine

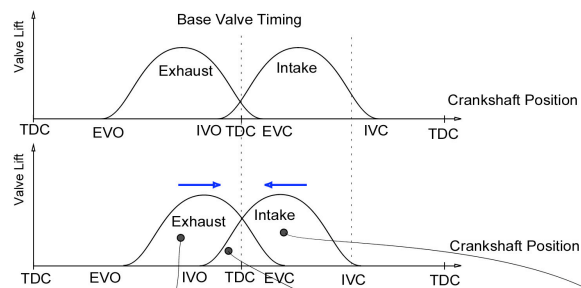
Intake and exhaust cam timing change independently based on operating conditions.

(Leone et al, SAE 960584

Jankovic, Magner, IFAC Congress, 2002)

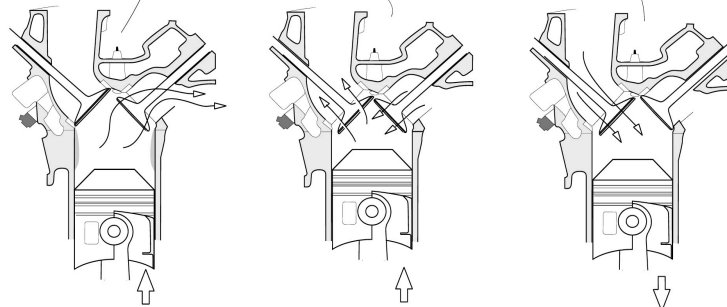


## Dual-independent VCT – high overlap regime



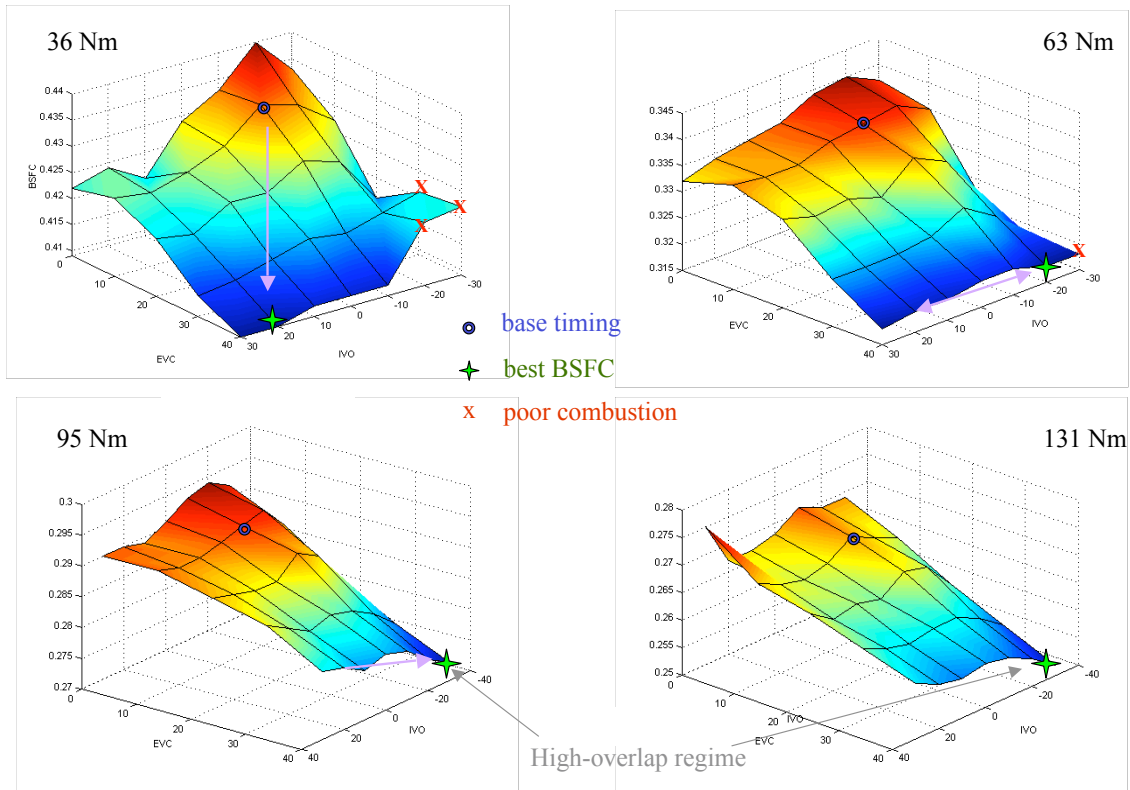
FE improvement through

- higher dilution
- higher compression

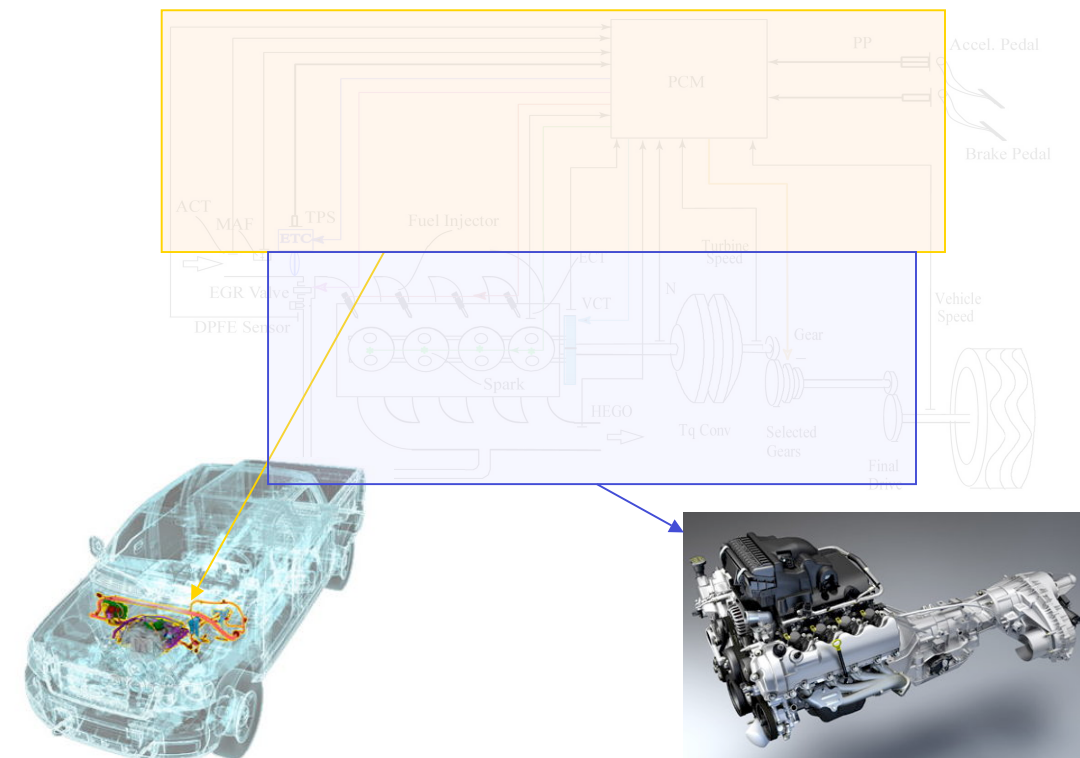




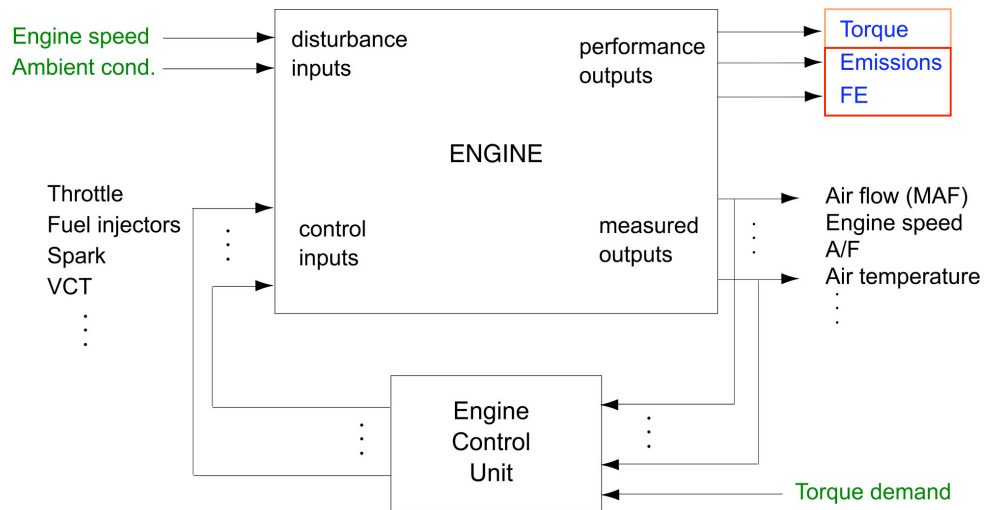
## BSFC vs IVO and EVC at MBT spark (1500 RPM)



## Powertrain control system – hardware configuration



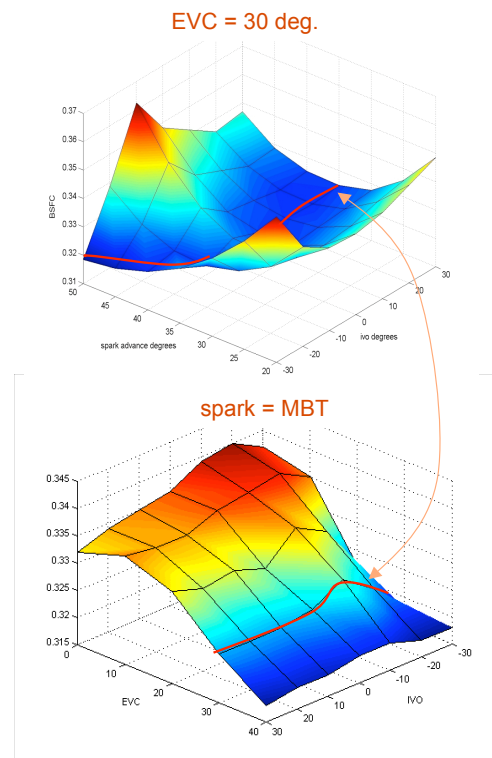
## Engine control system – control theoretic viewpoint



- Disturbances are measured/known
- Performance outputs are not measured
- Resulting control system relies on feedforward component

## Optimization vs set point regulation (di-VCT)

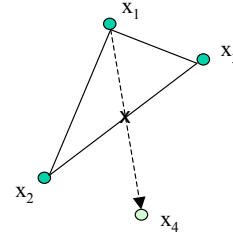
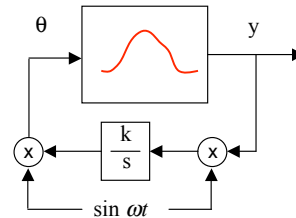
- performance output (cost) may be unmeasured
- (even if it is measured) set-points not available – the smaller the better.
- At the optimum, gain is 0
  - deviation on either side increases cost
- On an active constraint actuation becomes unidirectional.
- Instead of feedback regulation one can search for the optimum.



## On-line search for the optimum

Several approaches to search for the optimum based on real-time measurements:

- Extremum seeking (sinusoidal perturbation)  
(Ariyur & Krstic, Wiley, 2004)
- Direct search methods (e.g. Nelder-Mead)  
(Wright, *Numerical Analysis* 1995, Addison-Wesley  
Kolda et al, *SIAM Review*, 2003)
- Gradient search / stochastic approximation  
(Spall, *Wiley Encyclopedia of EE*, Volume 20, 1999  
Teel, *CDC 2000*, Sydney)



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## Gradient Search Methods

- Several GS methods experimentally tested on di-VCT engine
  - Modified Box-Wilson method (Box, Wilson, *J. Royal Stat. Soc.*, 1951)
  - Simultaneously Perturbed Stochastic Approximation
  - Persistently Exciting Finite Differences

### SPSA/PEFD algorithm

- Iteratively adjust parameters (*ivo*, *evc*, *spark*) to minimize a cost  $f(\theta)$  (i.e. BSFC):

1. Pick randomly or periodically one direction in  $\mathbb{R}^3$  among:

$$v_1 = [1 \ 1 \ 1], v_2 = [-1 \ 1 \ 1], v_3 = [1 \ -1 \ 1], v_4 = [1 \ 1 \ -1]$$

2. Assign  $\theta = \theta_k + \gamma v_k$ , measure  $f(\theta_k + \gamma v_k)$

3. Assign  $\theta = \theta_k - \gamma v_k$ , measure  $f(\theta_k - \gamma v_k)$

4. Calculate the next estimate:

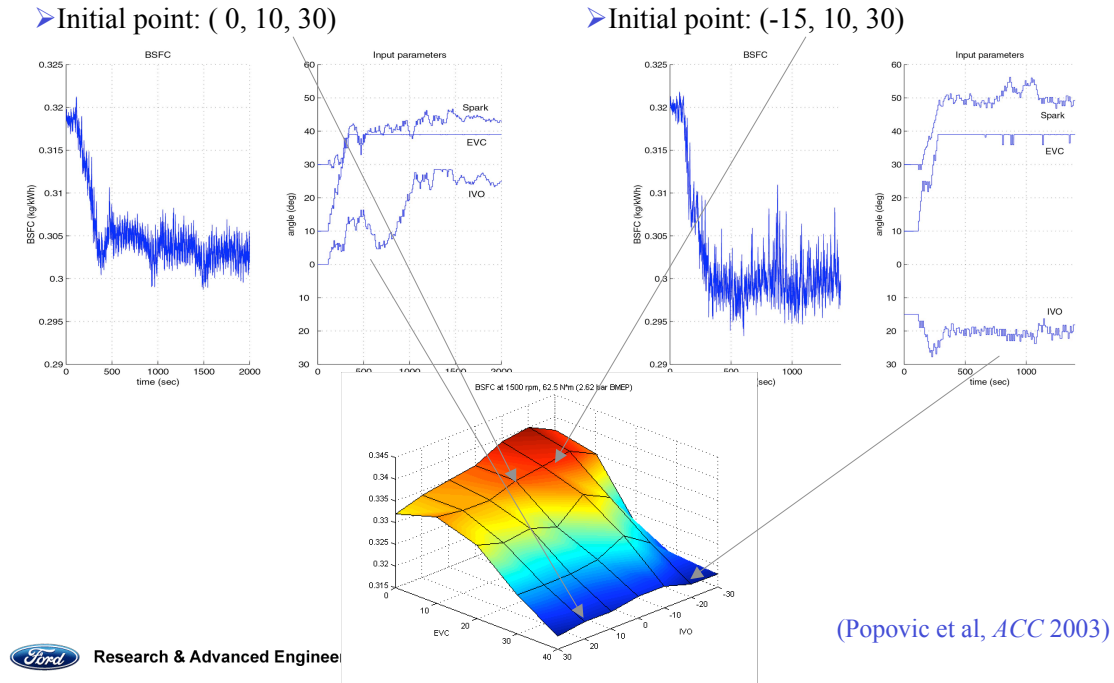
$$\theta_{k+1} = \theta_k + \alpha \cdot v_k \cdot \frac{f(\theta_k + \gamma v_k) - f(\theta_k - \gamma v_k)}{2\gamma}$$



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## Experimental results (SPSA algorithm results shown)

Testing at 1500 RPM, 63 Nm torque.



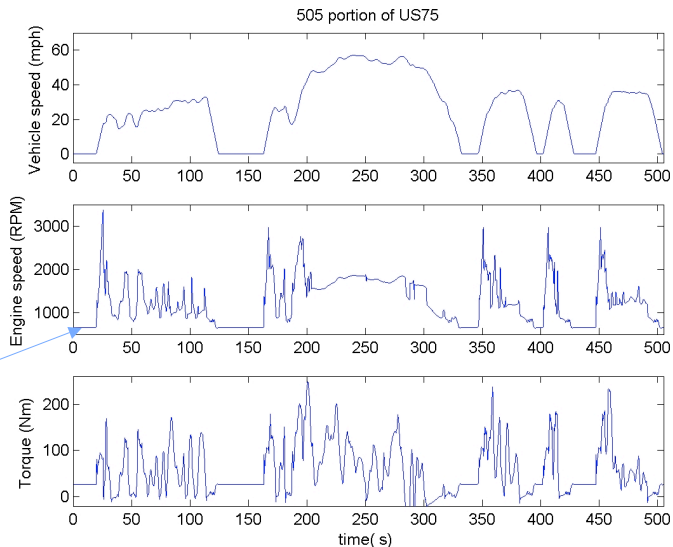
## Gradient search optimization – summary

- 15 minutes for GS to find the optimal point with 3 DoF
- 20 seconds just to find MBT spark (Dorey & Stewart, CCA, 1994)
- Not fast enough for on-the-road optimization.

Federal drive cycle prescribes the vehicle speed profile.

This constrains engine speed and torque as shown.

Prolonged speed/torque steady state found only in idle.



## Cycle optimization (off-line)

- FE optimization subject to emissions (and cycle RPM/torque) constraints

$$\begin{aligned} & \min_{(ivo, evc, spark)} \int_{\text{cycle}} \text{fuel consumption} \\ & \text{subject to } \int_{\text{cycle}} \text{emissions}(ivo, evc, spark) \leq \text{limit} \end{aligned}$$

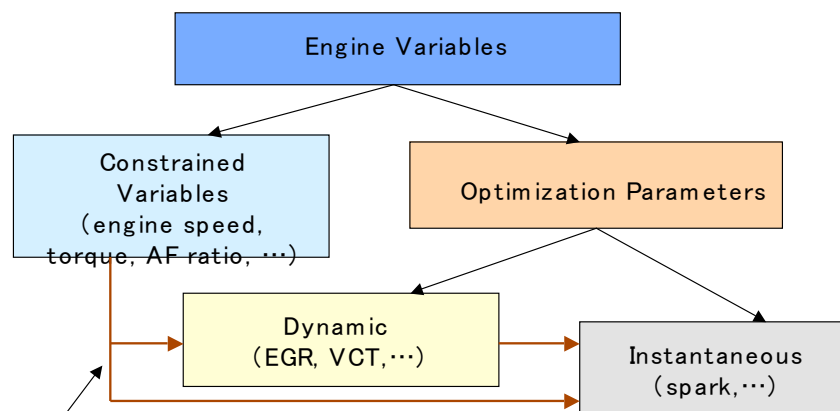
- Dynamic programming  $\longrightarrow$   $\left\{ \begin{array}{l} \text{(Auiler et al. SAE 770076)} \\ \text{Cohen et al. SAE 840544} \\ \text{Kolmanovsky et al. ACC 2002)} \end{array} \right.$ 
  - Engine and after-treatment models required
- Cycle-gradient optimization (Dohner, SAE 780286)
  - Alternates OL gradient computation & scheduled implementation –  $f(N, tq)$
- Point-wise FE optimization
  - if separate emissions (~first 30s) and FE modes are established.



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## Point-wise optimization

- At each speed/torque find the best combination of the optimization parameters
  - Note that this is not sufficient for transients operation



Scheduling:

$$\text{dynamic\_parameters} = f(\text{constrained\_variables})$$

$$\text{instantaneous\_parameters} = f(\text{constrained\_variables}, \text{dynamic\_parameters})$$



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## Full factorial optimization – cam and spark scheduling

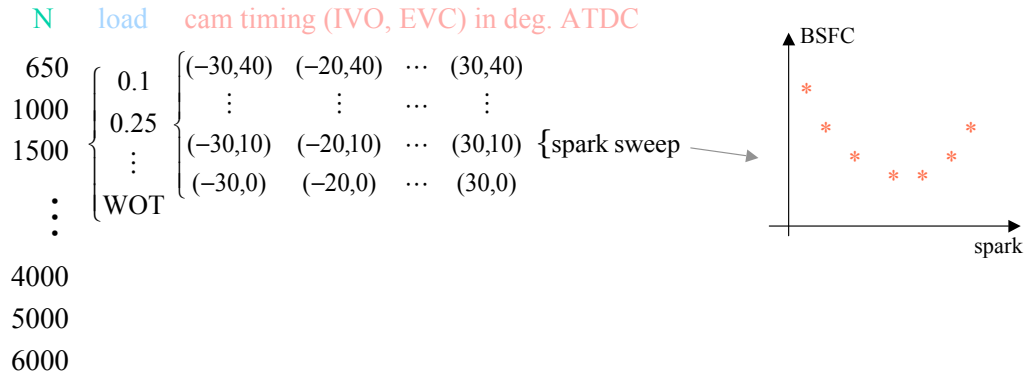
- FE benefit depends on the accuracy of the following ECU schedules

$$ivo = Fn\_ivo(N, tq)$$

$$evc = Fn\_evc(N, tq)$$

$$spark = Fn\_mbt(N, load, ivo, evc)$$

- Full factorial map:**



- 35-fold increase over conventional (fixed cam) – would take 15 months to complete.



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## Engine mapping and optimization – improving efficiency

- Industry standard – Design of Experiments (DOE)

(Montgomery, Wiley NY, 2001

NIST/SEMATECH e-Handbook of Statistical Methods)

- (D- or V-) optimal designs
  - use only a fraction of FF points
- Regressions generate “surfaces”
  - Polynomial
  - Radial basis function
- The regressed surfaces used to find optimal parameter schedules.
- “Black-box” approach, accuracy/complexity tradeoff



Box-Behnken Design for Three Factors



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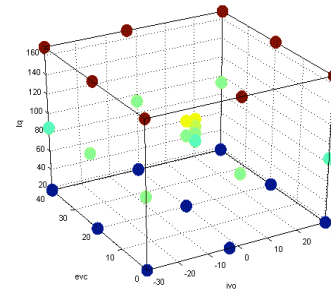
## 4D V-optimal design

### Approach 1

- V-optimal DOE in 4 dimensions (*speed, torque, ivo, evc*)
  - spark sweep at each selected point
- Matlab's Model Based Calibration tool generates mapping matrix
- di-VCT data regressed with a 3rd order polynomials in 4 variables:

$$bsfc / spark = \sum_{i+j+k+l+m=3} c_n \cdot N^i \cdot tq^j \cdot ivo^k \cdot evc^l \cdot 1^m$$

- Used 100 spark sweeps for 35 coefficients.



A V-optimal design for three factors



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## 2D Quadratic CCD (QCCD)

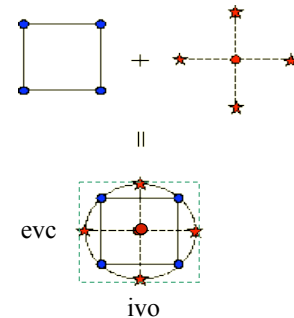
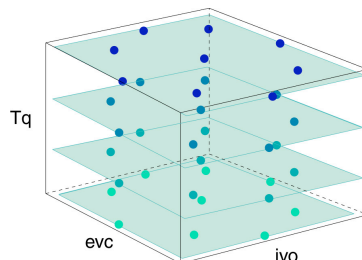
### Approach 2

- At each speed/torque the “response surfaces” assumed quadratic in IVO, EVC

$$bsfc / spark = a_0 + a_1 ivo + a_2 evc + a_3 ivo evc + a_4 ivo^2 + a_5 evc^2$$

Thus,  $a_i = a_i(N, load)$  (full factorial in N, load)

- At each speed/load map spark at 9 ivo/evc pairs (“central composite design – CCD”)



Box & Wilson CCD



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## Fuel economy comparisons (our data for di-VCT)

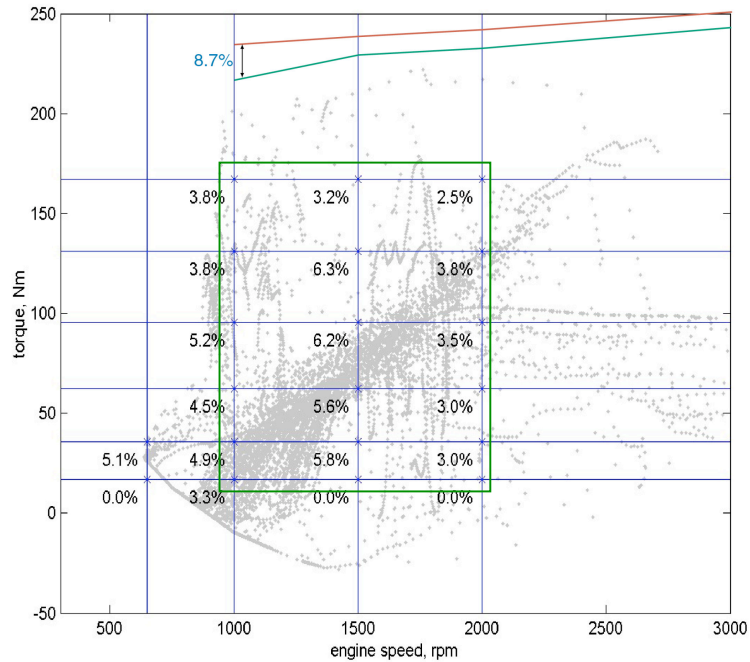
Each gray dot is a 0.1 second operation over the US75 cycle.

The numbers show % steady state FE improvement over the fixed base timing.

Drive cycle FE improvement prediction

**3.11%**

(assuming no FE improvement outside the rectangle)

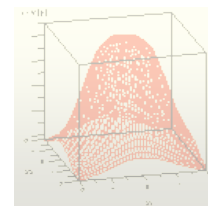


## FE penalty compared to full-factorial as a benchmark

	FE penalty	Number of spark sweeps*
Fixed cam at base timing (-10,10) deg ATDC	3.11%	18
4D V-optimal DOE	1.01%	100
Quadratic CCD	0.64%	162
Full-factorial	0%	630

\* For optimization over the rectangle (1000 to 2000 RPM x 16 to 167 Nm)

- 20% to 30% FE loss from the benefit potential
  - lower accuracy at the edges where the optimal points tend to be.
- Difficult to avoid in a DOE approach.



Information function (variance<sup>-1</sup>)  
for 2-D QCCD

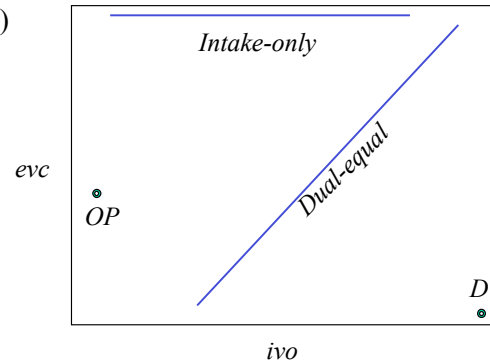
## Feature based guided mapping

- Basic idea – selectively map region(s) based on
  - a-priori knowledge
  - on-line optimization tests (e.g. gradient search)
- More than 90% of optimal points fall on two lines
  - Dual-equal line
  - Intake-only line
  - + OP and D points (for special conditions)

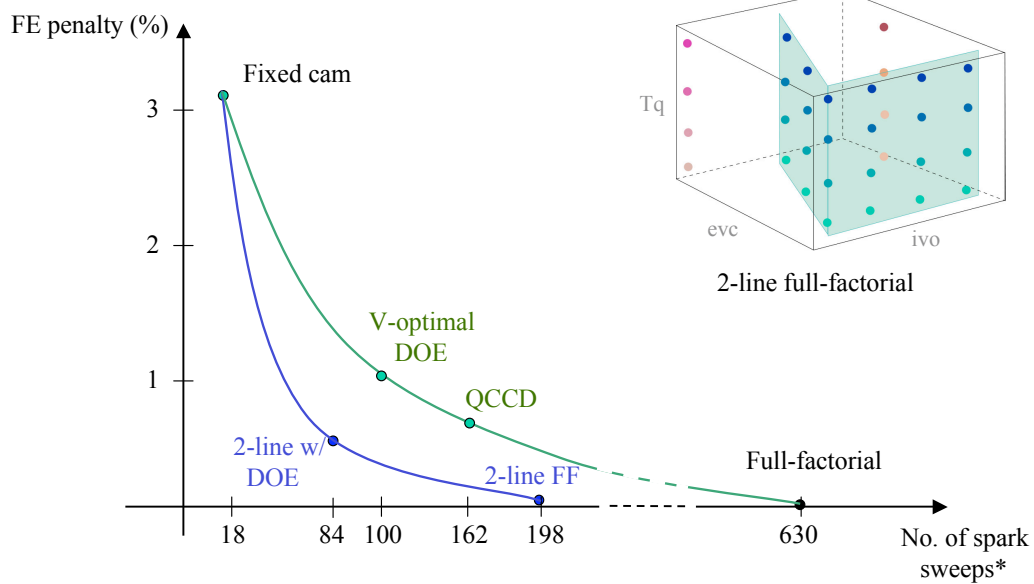
### Advantages

- higher accuracy on mapped features
- compatible with DOE

No point outside these features is mapped  
(what happens in transients?)



## Steady-state FE penalty and mapping effort



## Inverse distance interpolation for transients

- Nonparametric (**kernel**) methods (Hardle, Cambridge University Press, 1989)

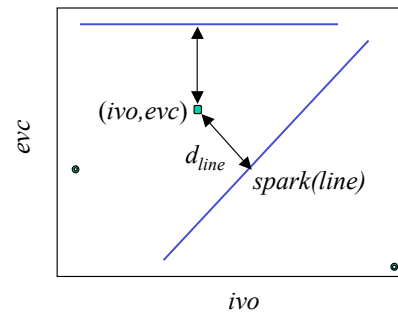
- Given data  $[X_i, Y_i]$  and a function  $K(u)$  (kernel) 
$$\hat{Y}(x) = \frac{\sum_i K(x-X_i)Y_i}{\sum_i K(x-X_i)}$$
  - Less efficient than parametric (e.g. polynomial) methods
  - Predictable in data poor regions
  - Calibration is local

- Inverse-distance kernel  $K(u)=1/(||u||^2+\epsilon)$

- Replaced points  $(X, Y)$  with (line) features

$$spark(ivo, evc) = \frac{\sum_j \frac{1}{(d_{line\_j}^2 + \epsilon)} \times spark(line_j)}{\sum_j \frac{1}{(d_{line\_j}^2 + \epsilon)}}$$

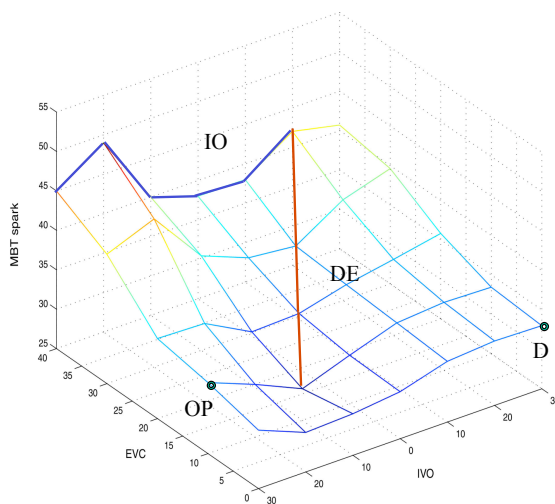
(Jankovic & Magner, ACC 2004)



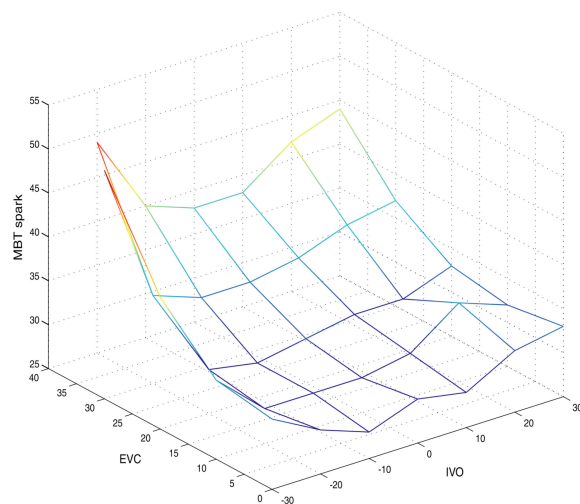
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## Comparison of MBT spark response surfaces

Surface generated by inv-dist from values at mapped features



Full factorial surface



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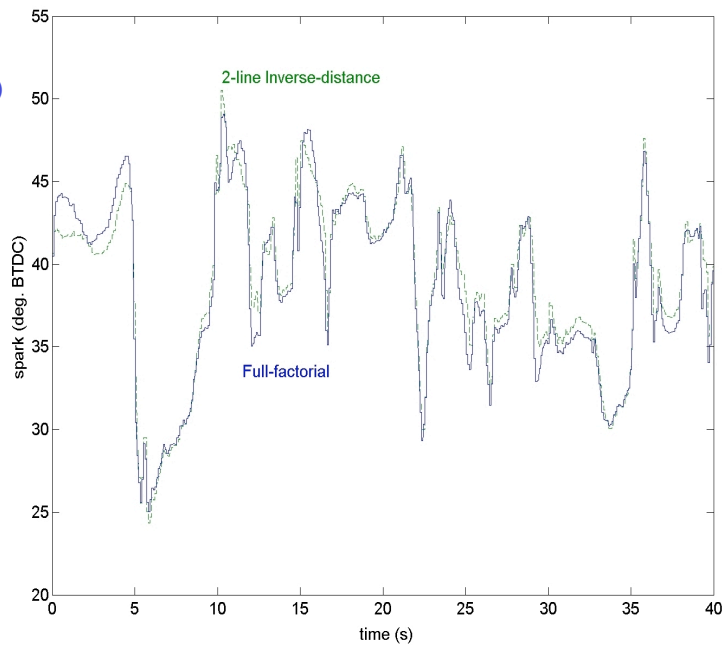
## Transient spark scheduling accuracy (40 sec. of the drive cycle)

### Vehicle data:

Full factorial (post-processed)

2-line inverse-distance  
(vehicle ECU)

FE penalty (transient)  
for 2-line ID → 0.04%



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## Vehicle tests

To test the approach in the vehicle we implemented 2-line + inv. dist.

### Fuel economy comparison (di-VCT versus fixed base cam timing)

- Drive cycle simulation prediction → 3.11%
- Vehicle tests (4+4 back to back tests) → 2.97%

If you are not convinced yet ...

Before



After



Our test vehicle with di-VCT engine

## Conclusion

- “It is difficult to specify and impossible to implement a general multivariable function even if the function is known” – Ho
  - For modeling/mapping, curse of dimensionality strikes early.
  - ES, direct, or gradient search too slow for on-the-road application.
- “All models are wrong, but some are useful,” – Box
  - full-factorial approach costly to map
  - explored mapping with reduced measurement set
    - DOE and guided (2-line) mapping compared.
- “The minimum is the result of the omission of the inessentials” – Powson
  - inverse-distance interpolation implemented, tested in-vehicle.

